## Modeling Rhythms on Differents Levels: Cells, Tissues, and Organisms



### Hanspeter Herzel

Institute for Theoretical Biology (ITB) Charité and Humboldt University Berlin

#### **Molecular Chronobiology**



# Clock genes and feedback loops

Proc. Nat. Acad. Sci. USA Vol. 68, No. 9, pp. 2112-2116, September 1971

#### **Clock Mutants of Drosophila melanogaster**

(eclosion/circadian/rhythms/X chromosome)

RONALD J. KONOPKA AND SEYMOUR BENZER

#### Feedback of the *Drosophila period* gene product on circadian cycling of its messenger RNA levels

Paul E. Hardin<sup>\*†</sup>, Jeffrey C. Hall<sup>†</sup> & Michael Rosbash<sup>\*†</sup>



# The core clock in Drosophila – negative and positive feedback



D. Bell-Pedersen et al. 2005

## The core clock in mammals



D. Bell-Pedersen et al. 2005

# Limits of quantitative models

single cells

#### models

advanced models of feedback loops incl. PER/CRY loops and RORE-loops



Relogio et al. PLoS Comp. Biol. 2011

#### data

- noisy reporter signals of at most 44 days
- few PRCs (mostly phase resetting)
- kinetic parameters mostly unknown



Abraham, Schlichting et al., in revision

# Limits of quantitative models

## modelseuronal networksata

network models with heterogeneity

different coupling schemes etc.



- movies with waves and tides
- multiple coupling mechanisms debated
- some PRCs (VIP, AVP, optogenetics...)
- splitting rare



# Limits of quantitative models

### moden organismic leval

#### COUPLED CIRCADIAN OSCILLATORS



J. theor. Biol. (1978) 70, 297-313

#### Two Coupled Oscillators: Simulations of the Circadian Pacemaker in Mammalian Activity Rhythms

SERGE DAAN<sup>†</sup> AND CHARLES BERDE

- long actograms
- many PRCs incl. dead zones
- entrainment/jetlag protocols
- saisonal variations



## Challenge

#### genetic feedback + coupling → network models models

## Challenge



regarding cells versus ensembles see also: Rougemont & Naef 2007; vanderLeest...Meijer 2009; Bordyugov et al. 2011; John,Taylor et al. 2014; Pia Rose 2015



#### Figure 4. Alignment of Neuronal Subgroup Responses to a Light Pulse Reveals Temporally Distinct Kinetic Signatures of Phase Retuning

In (A)–(C), plots of neuronal subgroup data are coded by color: s-LNv (red), I-LNv (yellow), LNd (orange), DN1 (blue), and DN3 (green).

(A) Top: average bioluminescence traces for subgroups maintained in DD exhibit a progressive and monotonic loss of rhythmicity and inter-subgroup synchrony over time. Bottom: after a LP, average bioluminescence traces for subgroups exhibit a transient reduction in rhythmic amplitude and intersubgroup synchrony, followed by a general strengthening of rhythmic amplitude and intersubgroup synchrony over time relative to corresponding neurons in DD.

## Complex network dynamics

#### Light Evokes Rapid Circadian Network Oscillator Desynchrony Followed by Gradual Phase Retuning of Synchrony

Logan Roberts,<sup>1</sup> Tanya L. Leise,<sup>2</sup> Takako Noguchi,<sup>3</sup> Alexis M. Galschiodt,<sup>1</sup> Jerry H. Houl,<sup>1</sup> David K. Welsh,<sup>3,4</sup> and Todd C. Holmes<sup>1,\*</sup>

#### Roberts et al., 2015, Current Biology 25, 858-867



Exposure of Cultured Brain Explants to a Light Pulse Reveals Qualitatively Distinct Dynamic Signatures of Neuronal Subgroups

## From cells to networks to organisms

- 1. Single cell rhythms: many detailed models but limited single cell data
- 2. Synchronization: sloppy oscillators useful, coupling phase matters
  - 3. Coupling makes oscillators "strong" (small PRCs, narrow entrainment range)
  - 4. Strong oscillators have flexible entrainment phases

## Some open questions

- How is fine-tuning of periods possible despite molecular noise (e.g. transcriptional bursts)?
- How long delays (6-12 hours needed) are realized?
- What are the most essential switches?
- How do transcriptional feedback loops interact with other oscillators (cell cycle, metabolism, peroxiredoxins)?
- Where are the feedbacks in the cyanobacterial clock?
- How to get robust synchronization and entrainment instead of splitting and chaos?

#### E-boxes, ROR-elements and D-boxes drive clock genes



H Ukai, HR Ueda: Annu Rev Physiol 72: 579-603 (2010)

#### Transcriptional Architecture and Chromatin Landscape of the Core Circadian Clock in Mammals

Nobuya Koike,<sup>1</sup> Seung-Hee Yoo,<sup>1</sup> Hung-Chung Huang,<sup>1</sup> Vivek Kumar,<sup>1</sup> Choogon Lee,<sup>2</sup> Tae-Kyung Kim,<sup>1</sup> Joseph S. Takahashi<sup>1,3\*</sup>



Science 19, 349-354,

#### Negative feedbacks as a common design principle



D. Bell-Pedersen et al. 2005

#### Delayed nuclear import in Drosophila P. Meyer, L. Saez, M. W. Young, Science 2006



J.C. Dunlap 2006

#### FASPS: Per phosphorylation controls delay

#### **Measurements**



Vanselow et al., Genes & Dev, 2006

## Huge protein complexes regulate transcription



Jin Young Kim et al.

#### Synergy of negative (orange) and positive (blue) regulations

Roles of Self-Activation, Cross-Activation and Saturable Degradation



B. Ananthasubramaniam et al. 2014

## Take home messages

- Delayed negative feedback are necessary but not sufficient for self-sustained oscillation
- Delays are tuned by transcription, translation, complex formation, phosphorylation, nuclear translocation, stability, epigenetics, ...
- Nonlinearities (switches) can result from cooperativity, positive feedbacks and sequestration
- Understanding synchronization and entrainment requires oscillator theory (PRCs, limit cycles, Arnold tongues....)

## Negative PER/CRY Loop in Early Models



## Both loops can generate



Relogio et al. PLoS Comp. Biol. 2011

#### Key role of the Rev-Erb loop

OPEN O ACCESS Freely available online

PLOS COMPUTATIONAL BIOLOGY

#### Tuning the Mammalian Circadian Clock: Robust Synergy of Two Loops

Angela Relógio<sup>1</sup>\*, Pal O. Westermark<sup>1</sup>, Thomas Wallach<sup>2</sup>, Katja Schellenberg<sup>2</sup>, Achim Kramer<sup>2</sup>, Hanspeter Herzel<sup>1</sup>

1 Institute for Theoretical Biology, Humboldt University, Berlin, Germany, 2 Laboratory of Chronobiology, Institute of Medical Immunology Charité - Universitätsmedizin Berlin, Berlin, Germany

#### Rev-erbα and Rev-erbβ coordinately protect the circadian clock and normal metabolic function

Anne Bugge, Dan Feng, Logan J. Everett, Erika R. Briggs, Shannon E. Mullican, Fenfen Wang, Jennifer Jager, and Mitchell A. Lazar<sup>1</sup>

LETTER

doi:10.1038/nature11048

### Regulation of circadian behaviour and metabolism by REV-ERB- $\alpha$ and REV-ERB- $\beta$

Han Cho<sup>1</sup>, Xuan Zhao<sup>1</sup>, Megumi Hatori<sup>2</sup>, Ruth T. Yu<sup>1</sup>, Grant D. Barish<sup>1</sup>, Michael T. Lam<sup>3</sup>, Ling-Wa Chong<sup>1</sup>, Luciano DiTacchio<sup>2</sup>, Annette R. Atkins<sup>1</sup>, Christopher K. Class<sup>3</sup>, Christopher Liddle<sup>4</sup>, Johan Auwerx<sup>5</sup>, Michael Downes<sup>1</sup>, Satchidananda Panda<sup>2</sup> & Ronald M. Evans<sup>1.6</sup>

ARTICLE

doi:10.1038/nature11030

#### Regulation of circadian behaviour and metabolism by synthetic REV-ERB agonists

Laura A. Solt<sup>1</sup>\*, Yongjun Wang<sup>1</sup>\*, Subhashis Banerjee<sup>1</sup>, Travis Hughes<sup>1</sup>, Douglas J. Kojetin<sup>1</sup>, Thomas Lundasen<sup>1</sup>, Youseung Shin<sup>2</sup>, Jin Liu<sup>1</sup>, Michael D. Cameron<sup>2</sup>, Romain Noel<sup>2</sup>, Seung–Hee Yoo<sup>3</sup>, Joseph S. Takahashi<sup>3</sup>, Andrew A. Butler<sup>4</sup>, Theodore M. Kamenecka<sup>2</sup> & Thomas P. Burris<sup>1,5</sup>

by courtesy of Marc Lefranc

## Construction of a core clock model using

- representative genes: activators (Bmal1, Dbp)+ early inhibitors (Per2, Rev-Erb)+late inhibitor (Cry1)
- experimentally verified binding sites
- known degradation rates
- reasonable delays
- fitted transcriptional parameters

## Regulatory elements in clock gene promoters



#### **Expression profiles in liver & adrenal gland**



Circadian time [h]

A. Korencic et al., Scientific Reports 4:5782 (2014)

#### **Core-clock model from expression profiles and promoters**



Anja Korencic et al., Scientific Reports 2014

## Quantitative agreement of experimental data and simulations with DDEs

Expression profiles were fitted by sinusoidal functions with harmonics

 $\frac{\mathrm{d}[Bmal1]}{\mathrm{d}t} = \left(\frac{a}{ak + [Rev - erba]_{\tau_{Reverba}}}\right)^2 - d_{Bmal1} \cdot [Bmal1]$ etc

Simulations



### Multiple loops can generate sustained rhythms



Figure 1: (A) Network graph of the model. Activating and inhibiting influences between genes are colored in blue and red respectively. (B) Simulation of gene expression of all 5 genes. (C) Simulation of gene expression of *Rev-Erba* and *Bmal1*, with other genes fixed to their constant mean value from figure A. After a slight increase of the activation strengh of *Bmal1* to *Rev-Erba*, oscillations are regained with a period of 24h. (D) Simulation of gene expression of *Rev-Erba*, *Per2* and *Cry1*, with other genes fixed to their constant mean value from figure A. The period increases to 27h, but oscillations are retained.

Patrick

## What are the most essential regulations?

- we test ON/OFF configurations of 17 regulations
- OFF: regulatory term is clamped to its mean
- out of 131072 configurations 14125 are rhythmic
- percentage of ON relates to relevance of regulation
- e.g. cyclic activation of Per2 is ON for only 2.99% but Rev-Erb inhibits Cry1 in 94.26%

### Frequencies of Cyclic Regulatory Interactions



## "Repressilator genes" are essential for clock

#### LETTER

doi:10.1038/nature11048

#### Regulation of circadian behaviour and metabolism by REV-ERB- $\alpha$ and REV-ERB- $\beta$

Han Cho<sup>1</sup>, Xuan Zhao<sup>1</sup>, Megumi Hatori<sup>2</sup>, Ruth T. Yu<sup>1</sup>, Grant D. Barish<sup>1</sup>, Michael T. Lam<sup>3</sup>, Ling–Wa Chong<sup>1</sup>, Luciano DiTacchio<sup>2</sup>, Annette R. Atkins<sup>1</sup>, Christopher K. Glass<sup>3</sup>, Christopher Liddle<sup>4</sup>, Johan Auwerx<sup>5</sup>, Michael Downes<sup>1</sup>, Satchidananda Panda<sup>2</sup> & Ronald M. Evans<sup>1.6</sup>

The circadian clock acts at the genomic level to coordinate internal behavioural and physiological rhythms via the CLOCK-BMAL1 transcriptional heterodimer. Although the nuclear receptors REV-ERB-a and REV-ERB-B have been proposed to form an accessory feedback loop that contributes to clock function<sup>1,2</sup>, their precise roles and importance remain unresolved. To establish their regulatory potential, we determined the genome-wide cis-acting targets (cistromes) of both REV-ERB isoforms in murine liver, which revealed shared recognition at over 50% of their total DNA binding sites and extensive overlap with the master circadian regulator BMAL1. Although REV-ERB-a has been shown to regulate Bmal1 expression directly<sup>1,2</sup>, our cistromic analysis reveals a more profound connection between BMAL1 and the REV-ERB-a and REV-ERB-ß genomic regulatory circuits than was previously suspected. Genes within the intersection of the BMAL1, REV-ERB-a and REV-ERB-ß cistromes are highly enriched for both clock and metabolic functions. As predicted by the cistromic analysis, dual depletion of Rev-erb- $\alpha$  and Rev-erb- $\beta$  function by creating doubleknockout mice profoundly disrupted circadian expression of core circadian clock and lipid homeostatic gene networks. As a result, double-knockout mice show markedly altered circadian wheelrunning behaviour and deregulated lipid metabolism. These data

#### Mammalian Cry1 and Cry2 are essential for maintenance of circadian rhythms

Gijsbertus T. J. van der Horst∗, Manja Muijtjens∗, Kumiko Kobayashi⁺, Riya Takano↑, Shin-ichiro Kanno↑, Masashi Takao↑, Jan de Wit∗, Anton Verkerk∗, Andre P. M. Eker∗, Dik van Leenen‡, Ruud Buijs§, Dirk Bootsma∗, Jan H. J. Hoeijmakers∗ & Akira Yasui↑

\* MGC, Department of Cell Biology and Genetics, Erasmus University, PO Box 1738, 3000 DR Rotterdam, The Netherlands

† Department of Molecular Genetics, Institute of Development, Aging and Cancer, Tohoku University, 980-8575 Sendai, Japan

100000 University, 500-5575 senata, jupan ‡ MGC, Department of Clinical Genetics, Easmus University, PO Box 1738, 3000 DR Rotterdam, The Netherlands

§ Netherlands Institute for Brain Research, Meibergdreef 33, 1105 AZ Amsterdam, The Netherlands

Many biochemical, physiological and behavioural processes show circadian rhythms which are generated by an internal timekeeping mechanism referred to as the biological clock. According to rapidly developing models, the core oscillator driving this clock is composed of an autoregulatory transcription-(post) translation-based feedback loop involving a set of 'clock' genes<sup>1-6</sup>. Molecular clocks do not oscillate with an exact 24-hour rhythmicity but are entrained to solar day/night rhythms by light. The mammalian proteins Cry1 and Cry2, which are members of the family of plant blue-light receptors (cryptochromes) and photolyases, have been proposed as candidate light receptors for photoentrainment of the biological clock7-10. Here we show that mice lacking the Cry1 or Cry2 protein display accelerated and delayed free-running periodicity of locomotor activity, respectively. Strikingly, in the absence of both proteins, an instantaneous and complete loss of free-running rhythmicity is observed. This suggests that, in addition to a possible photoreceptor and antagonistic clock-adjusting function, both proteins are essential for the maintenance of circadian rhythmicity.

Cell, Vol. 105, 683-694, June 1, 2001, Copyright ©2001 by Cell Press

#### Nonredundant Roles of the *mPer1* and *mPer2* Genes in the Mammalian Circadian Clock

Binhai Zheng,<sup>1,5</sup> Urs Albrecht,<sup>2,7</sup> Krista Kaasik,<sup>1</sup> Marijke Sage,<sup>1</sup> Weiqin Lu,<sup>1</sup> Sukeshi Vaishnav,<sup>1,3</sup> Qiu Li,<sup>1</sup> Zhong Sheng Sun,<sup>1,3</sup> Gregor Eichele,<sup>2,8</sup> Allan Bradley,<sup>1,3,4,9</sup> and Cheng Chi Lee<sup>1,4</sup> <sup>1</sup> Department of Molecular and Human Genetics <sup>2</sup> Verna and Marrs McLean Department of Biochemistry <sup>3</sup> Howard Hughes Medical Institute Baylor College of Medicine One Baylor Plaza Houston. Texas 77030

#### Summary

Mice carrying a null mutation in the Period 1 (mPer1) gene were generated using embryonic stem cell technology. Homozygous mPer1 mutants display a shorter circadian period with reduced precision and stability. Mice deficient in both mPer1 and mPer2 do not express circadian rhythms. While mPER2 regulates clock gene expression at the transcriptional level, mPER1 is dispensable for the rhythmic RNA expression of mPer1 and mPer2 and may instead regulate mPER2 at a posttranscriptional level. Studies of clock-controlled genes (CCGs) reveal a complex pattern of regulation by mPER1 and mPER2, suggesting independent controls by the two proteins over some output pathways. Genes encoding key enzymes in heme biosynthesis are under circadian control and are regulated by mPER1 and mPER2. Together, our studies show that mPER1 and mPER2 have distinct and complementary roles in the mouse clock mechanism.

pervasive role in temporal organization of biochemical and physiological functions (Young, 2000).

The first clock mutants were isolated in Drosophila (Konopka and Benzer, 1971) and the corresponding molecular defects were later identified in the Period (per) gene (Bargiello et al., 1984), Since then, a number of additional clock genes, including timeless (tim), clock (clk), cvcle (cvc), doubletime (dbt), crvptochrome (crv), and recently vrille (vri), have been identified in this model organism (Allada et al., 1998; Blau and Young, 1999; Kloss et al., 1998; Myers et al., 1995; Rutila et al., 1998). Mutations in these genes alter the period length and/or lead to behavioral arrhythmicity. At the molecular level, the clock is characterized by the oscillating expression of specific clock genes including per and tim (Young, 2000). This oscillating expression is driven by an autoregulatory negative feedback loop where CLK and CYC act positively to drive the expression of per and tim. while PER and TIM act as a complex to regulate their own transcription negatively by inhibiting CLK/CYC (Allada et al., 1998: Darlington et al., 1998: Rutila et al., 1998). The cyclical activity of PER and TIM is also controlled posttranslationally by regulation of phosphorylation that involves the kinase DBT and nuclear entry (Kloss et al., 1998).

Orthologs of most *Drosophila* circadian clock genes have been identified in mammals, highlighting a general conservation in the clock mechanism between insects and mammals. In particular, three mammalian *Period* genes (*mPer1*, *mPer2*, and *mPer3*), two *Cryptochrome* genes (*mCry1* and *mCry2*), as well as *Clock*, *Bmal1* (ortholog to *Cyc*), and *CK1* $\epsilon$  (ortholog to *Dbt*) have been identified (Albrecht et al., 1997a; Bunger et al., 2000;

#### Mammalian Period represses and de-represses transcription by displacing CLOCK–BMAL1 from promoters in a Cryptochrome-dependent manner

Yi-Ying Chiou<sup>a,1</sup>, Yanyan Yang<sup>a,1</sup>, Naim Rashid<sup>b,c,1</sup>, Rui Ye<sup>a</sup>, Christopher P. Selby<sup>a</sup>, and Aziz Sancar<sup>a,c,2</sup>

<sup>a</sup>Department of Biochemistry and Biophysics, University of North Carolina School of Medicine, Chapel Hill, NC 27599; <sup>b</sup>Department of Biostatistics, University of North Carolina, Chapel Hill, NC 27599; and <sup>c</sup>Lineberger Comprehensive Cancer Center, University of North Carolina, Chapel Hill, NC 27599



Serial repression via Cry1, Rev-Erba, and Per2 confirmed

## Lessons from Modeling

#### How to design a minimal core clock model?

- Five genes represent most regulations
- DDEs require few parameters
- Transcriptional regulations remain heuristic
- Per/Cry loop, Rev-Erba loop and repressilator possible

# Synchronization of sloppy oscillators

## Sloppy oscillators synchronize well independent of specific coupling

concentration

mRNA

K=0.3

120 144

time (h)

48 60 72 d

96

2.5 r C

2

0.5

0

60 r **D** 

of oscillators

her

045 Per/Cry mRNA concentration

12 24 36 48 60 72

K=0.9

192 216

168

time (h)

40

20

20

1.5

0!

0

22 24

48

period (h)

24.3±1.22

26

144 192 240 288

time (h)



S. Bernard, D. Gonze, B. Cajavec, H. Herzel, and A. Kramer: Synchronization-Induced Rhythmicity of Circadian Oscillators in the Suprachiasmatic Nucleus, PLoS Comp. Biol. (2007) 3:e68.

## Damped oscillators synchronize well independent of specific coupling



S. Bernard, D. Gonze, B. Cajavec, H. Herzel, and A. Kramer: Synchronization-Induced Rhythmicity of Circadian Oscillators in the Suprachiasmatic Nucleus, PLoS Comp. Biol. (2007) 3:e68.



### Intrinsic, nondeterministic circadian rhythm generation in identified mammalian neurons

Alexis B. Webb<sup>a</sup>, Nikhil Angelo<sup>a</sup>, James E. Huettner<sup>b</sup>, and Erik D. Herzog<sup>a,1</sup>

makers. Instead, these results indicate that AVP, VIP, and other SCN neurons are intrinsic but unstable circadian oscillators that rely on network interactions to stabilize their otherwise noisy cycling.

## Coupling **phase** controls synchronization



Implications for dual role of GABA (J. Evans, Neuron 2013) and synchrony of neonatal versus adult SCN slices (Honma, Nature Communications 2013)

B. Ananthasubramaniam, E. D. Herzog, H. Herzel. PLoS Comp. Biol. 2014

#### **Coupling can even synchronize Cry-DKO neonatal SCN**



D. Ono, S. Honma, K. Honma Nature Communications 2013

#### Synchronization of noisy oscillators (WT and DKO)



CV about 1

CV above 1

Better sync for WT

Coupling strength enhances sync

Coupling phase matters strongly

I.T.Tokuda et al. Biophys J.



The environmental external oscillator

entrains our internal oscillator (the circadian clock)

#### The organization of the circadian system



@ 2001 Sinauer Associates, Inc



### The circadian oscillator



Reppert and Weaver, 2001